

大同大學 103 學年度研究所碩士班入學考試試題

考試科目: 控制系統

所別: 電機工程研究所

第1頁共1頁

註: 本次考試 不可以參考自己的書籍及筆記; 不可以使用字典; 不可以使用計算器。

1. Consider the feedback control system shown in Fig. P-1, where $Y(s)$ is the output, $R(s)$ is the input, and $D(s) = k \frac{s+z}{10s+1}$ is the compensator, for which k and z are two constants to be determined.

- (a) (5%) Please find the transfer function $G(s) = Y(s)/R(s)$.
- (b) (10%) Use Routh's criterion to determine the region in the k versus z plane for which the system is BIBO stable (Use k as the horizontal axis and z as the vertical axis.)
- (c) (10%) From (a) and (b), what conditions must k and z satisfy so that the system is stable and its output can track a unit step reference input with constant steady-state error?
- (d) (10%) From (a) and (b), please find k and z so that the closed-loop system poles are located at $s = -2 \pm j\sqrt{2}$.
- (e) (10%) Sketch the asymptotes for $D(s)$ with k and z given from (d) according to Bode plot rules.
- (f) (5%) From (e), is $D(s)$ the lead or lag compensator? Explain your answer and simple lead and lag will not be granted any point.

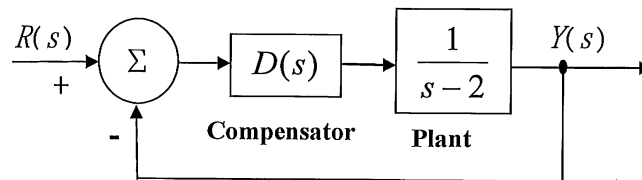


Fig. P-1

2. Consider the continuous-time system with the following differential equation

$$\ddot{y}(t) = u(t)$$

- (a) (15%) Determine the state-space representation of the above continuous-time system.
- (b) (15%) Determine a state-feedback controller such that the characteristic equation of the closed-loop system is $s^2 + a_1s + a_2 = 0$. (in terms of a_1 and a_2)

3. Consider the discrete-time system

$$y(k+2) + 0.6y(k+1) = u(k)$$

where $y(k)$ is the system output and $u(k)$ is the input.

- (a) (10%) For which values of P in the proportional controller

$$u(k) = P[r(k) - y(k)]$$

is the closed-loop system stable, where $r(k)$ is the reference input?

- (b) (10%) Determine the stationary error $r(k) - y(k)$ when $r(k)$ is a unit step function and when $P = 1$ in the controller as shown in (a).